

Functions

Functions

Splitting programs code into meaningful pieces (functions)
reduces time for debugging and maintaining

function: sequence of statements that perform a specific task
identified by a name

compound statement:

- **header**

begins with keyword `def`
ends with a colon (`:`)

- **body**

indented statements
includes a `return` statement

```
def function_name(formal parameters list):  
    statements  
    return returned expressions list
```

2 keywords: `def`, `return`
usual indentation: 4 spaces

Functions

```
def function_name(formal parameters list):  
    statements  
    return returned expressions list
```

returned expressions list:

- computed results
- variables, values, expressions
- parenthesis not required
- comma separated items
- can be empty

formal parameters list:

- function is defined formally with them (data)
- variable names, no values, no expressions
- parenthesis required
- comma separated values
- can be empty

return statement: the last executed statement (not necessarily the bottom-most)

module: file with one or more functions

Calling a function

a function is executed when it is **called (invoked)**:
syntax of the **call statement** or **function call**:

```
variables list = function_name (actual parameters list)
```

variables list:

- are assigned the returned values
- variable names, no values, no expressions
- parenthesis not required

actual parameters list:

- specific values to apply the function
- variable names, values, or expressions
- parenthesis required

formal versus **actual** parameters lists } **positional** correspondence
returned expressions versus variables lists }

Exercise 1

Problem definition: A body moves with an uniformly accelerated rectilinear motion with an acceleration \mathbf{a} , an initial velocity \mathbf{v}_0 and an initial position \mathbf{x}_0 . Units are meters and seconds. Write function `uarm` that takes these three parameters and a fourth one corresponding to a time, \mathbf{t} , and returns the final position and velocity of the body \mathbf{t} seconds after the motion start. Save this function in file `uarm.py`

Exercise 1

Problem definition: A body moves with an uniformly accelerated rectilinear motion with an acceleration \mathbf{a} , an initial velocity \mathbf{v}_0 and an initial position \mathbf{x}_0 . Units are meters and seconds.

Write function `uarm` that takes these three parameters and a fourth one corresponding to a time, \mathbf{t} , and returns the final position and velocity of the body \mathbf{t} seconds after the motion start.

header:

keyword `def`

given function name

formal parameters list: 4 parameters

ending colon (`:`)

body:

indented assignment statements

local variables `v`, `x`

```
def uarm (a, v0, x0, t) :  
    v = v0 + a*t  
    x = x0 + v0*t + 0.5*a*t**2  
    return v, x
```

return statement:

keyword `return`

returned expressions list: 2 variables

Exercise 1

```
def uarm (a, v0, x0, t) :  
    return v0 + a*t, x0 + v0*t + 0.5*a*t**2
```

Version with returned expressions:
body: only the return statement
returned expression list: 2 expressions
separated by a comma

file `test-uarm.txt`

```
>>> from uarm import uarm  
>>> uarm(1.1, 10.4, 3, 10) # actual parameters list: 4 values  
(21.4, 162.0)  
>>> uarm(2.1, 30/3.6, 100, 20) # actual parameters list: 3 values, 1 expression  
(50.333333333333336, 686.6666666666667)  
>>> vel, pos = uarm(2.1, 30/3.6, 100, 20) # 2 vars are assigned 2 returned expr  
>>> round(vel,2), round(pos,2) # rounded  
(50.33, 686.67)  
>>> a = 0.4  
>>> b = 2.3  
>>> c = 200  
>>> d = 15  
>>> vel, pos = uarm(a, b, c, d) # actual parameters list: 4 variables  
>>> round(vel,2), round(pos,2)  
(8.3, 279.5)
```

Flow of control

a function can call and be called by other functions

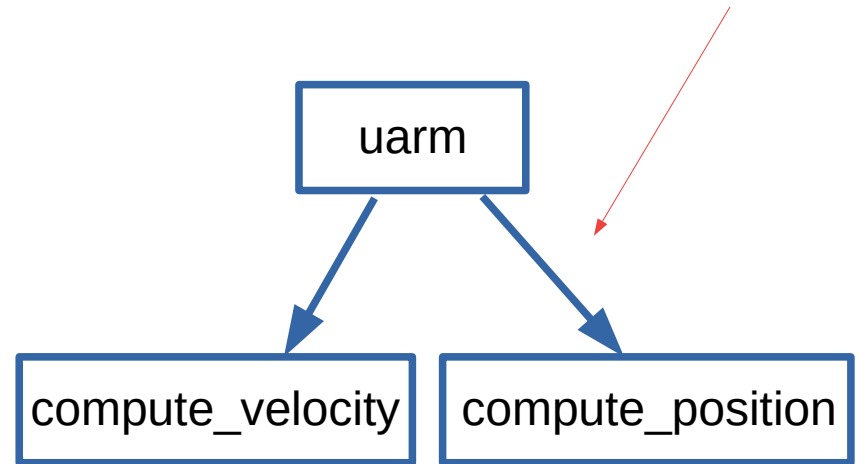
function A calls function B → function B gets the control

function B executes the return statement → function A recovers the control

Version of exercise 1 using 2 auxiliary functions:

```
def uarm (a, v0, x0, t):  
    v = compute_velocity(a, v0, t)  
    x = compute_position(a, v0, x0, t)  
    return v, x  
  
def compute_velocity(a, v0, t):  
    return v0 + a*t  
  
def compute_position(a, v0, x0, t):  
    return x0 + v0*t + 0.5*a*t**2
```

Flow of control represented by a directed (acyclic) graph



Exercise 2

Problem definition: write function `is_a_root` that takes four parameters **a**, **b**, **c** and **x**, corresponding to the coefficients of a quadratic equation, $ax^2+bx+c = 0$, and a candidate root **x**, and returns `True` if **x** is a root of the quadratic equation and `False` otherwise.

```
>>> is_a_root(1, 2, 1, -1)
True
>>> is_a_root(1, 2, 1, 3)
False
```

Exercise 2

Problem definition: write function `is_a_root` that takes four parameters `a`, `b`, `c` and `x`, corresponding to the coefficients of a quadratic equation, $ax^2+bx+c = 0$, and a candidate root `x`, and returns `True` if `x` is a root of the quadratic equation and `False` otherwise.

```
def is_a_root(a, b, c, x):  
    return a*x**2+b*x+c == 0
```

Boolean expression:
`is_a_root` is a Boolean function

```
>>> is_a_root(1, 2, 1, -1)  
True  
>>> is_a_root(1, 2, 1, 3)  
False
```

Exercise 2

Consider the equation $x^2 - 10.88 = 0$

```
>>> import math
>>> round(math.sqrt(10.88), 2)
3.2984845004941286
>>> is_a_root(1, 0, -10.88, 3.29)
False
```

```
def is_a_root_2(a, b, c, x, epsilon):
    return abs(a*x**2+b*x+c) <= epsilon
```

```
>>> is_a_root_2(1, 0, -10.88, 3.3, 0.01) # using epsilon = 0.01
True
>>> is_a_root_2(1, 0, -10.88, 3.3, 0.001) # epsilon = 0.001 value too small
False
>>> is_a_root_2(1, 0, -10.88, 3.2984, 0.001)
True
```

float comparisons:
precision problems
solved with a given precision epsilon